Electronic and phonon instabilities in face-centered-cubic alkali metals under pressure studied using ab initio calculations

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The evolution of Fermi surfaces and lattice dynamics for alkali metals in the fcc structure with pressure have been studied using ab initio calculations within the density functional theory. Fermi surface nesting features along the Γ–K symmetry direction in the Brillouin zone have been identified for Li, K, Rb, and Cs, while it is absent for Na. Moreover, a transverse acoustic phonon softening along the Γ–K with pressure is predicted for Li, Na, K, Rb, and Cs. This observation suggests a common phonon softening behavior in fcc alkali metals at high pressure. Analysis of the theoretical results suggests that the consideration of both phonon and electronic instabilities is crucial to the understanding of pressure-induced phase transitions in the fcc alkali metals.

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Alkali metals are usually considered as simple metals because of the simple electronic structure with just one conduction electron outside the closed-shell configurations. The nearly free electron model is known to be a good approximation to describe their electronic properties due to the weak interaction between valence electrons and ionic core under ambient conditions.1 However, under high pressure, the nearly free electron description of alkali metals fails as evidenced by the complex sequence of phase transitions.2 Alkali metals having the bcc structure at low pressure transform to an fcc modification for Li at 7.5 GPa,3 Na at 65 GPa,4 K at 11.5 GPa,5 Rb at 7 GPa,6 and Cs at 2.3 GPa,7 respectively. The bcc→fcc transition in alkali metals has been attributed to s→d electrons transfer for K, Rb, and Cs, and s→p electrons transfer for Li.8 At higher pressure all alkali metals with fcc structure transform into more complex structures. Specifically, Li at 39 GPa,9 Na at 103 GPa,4 K at 19 GPa,10 Rb at 13 GPa,11 and Cs at 4.2 GPa,12 transform to R-3m,9 I-43d,13 host-guest composite structure,10 C2221,11 and C2221 (Ref. 12) structures, respectively.

Very recently, several theoretical studies14–18 have contributed to the understanding of the enhanced superconducting transition temperature \( T_c \) with increasing pressure for fcc Li. It is now accepted that the combination of a Fermi surface nesting (FSN) with a transverse acoustic (TA) phonon softening along the Γ→K symmetry direction is responsible for the relatively high \( T_c \) for fcc Li.14,15 at high pressure. Moreover, the possible superconductivities in Na and K have been predicted theoretically by Sanna et al.16 for K and Shi and Papaconstantopoulos18,19 for K and Rb, respectively. Much experimental effort is needed to clarify the validity of these theoretical predictions. However, the physical mechanism driving the phase transition from fcc to the complex structures in alkali metals is less studied. Electronic (FSN)20 and dynamic instabilities21 are often responsible for phase transitions under pressure. In a previous study on fcc Cs,22 a softening of the TA phonons near the zone center was identified and attributed to the transition mechanism for the fcc \( Fm-3m \) to \( C222_1 \) phase transition. Recently, Rodriguez-Prieto and Bergara23 suggested that an FSN at 30 GPa could be the origin of the complex phase transitions for fcc lithium. In this work, we investigate systematically the evolution of Fermi surface and lattice dynamics with pressure in alkali metals with the fcc structure in order to probe the nature of the phase transition to high-pressure complex structures. We found a TA phonon softening along the Γ–K symmetry direction with pressure in all fcc alkali metals. Besides Li, FSN along Γ–K in the Brillouin zone (BZ) is also identified for K, Rb, and Cs, while it is absent for Na. It is shown that both the TA phonon softening and FSN are closely related to the phase transitions.

Lattice dynamics for alkali metals at high pressure are investigated using the pseudopotential plane-wave (PP) density-functional linear-response method.24 The local density approximation (LDA) exchange-correlation functional is employed.25 The Troullier-Martins (TM)26 norm-conserving scheme is used to generate a tight pseudopotential for Li, Na, K, Rb, and Cs with the electronic configurations of \( 2s^2 2p^6 \) for Li, \( 3s^2 3p^6 \) for Na, \( 4s^2 4p^6 \) for K, \( 5s^2 5p^6 \) for Rb, and \( 6s^2 6p^6 \) for Cs, respectively. Convergence tests gave a kinetic energy cutoff, \( E_{\text{cutoff}} \), as 80 Ry and a \( 16 \times 16 \times 16 \) Monkhorst-Pack (MP) grid for the electronic BZ integration. A \( 16 \times 16 \times 16 \) MP \( k \) mesh was found to yield phonon frequencies converged to within 0.05 THz. Fermi surface calculations for alkali metals are performed using the full-potential (FP) linearized augmented plane wave method, through WIEN2k,27 within the density functional theory (DFT).28 The electron exchange-correlation energy is described in the generalized gradient approximation (GGA).29 The cutoff of the plane-wave expansion was given by \( RK_{\text{max}} = 9 \). Convergence tests gave the use of 10 000 \( k \) points for the self-consistent calculation in the BZ. A large set of 32 768 \( k \) points was chosen for the calculation of the Fermi surfaces.

The theoretical equilibrium lattice constants and equation of states (EOS) of the fcc structure for the alkali metals studied here were determined by fitting the total energies as a function of volume to the 3rd-order Birch-Murnahan EOS.30 The calculated equilibrium lattice parameters \( (a_0) \), bulk
TABLE I. Calculated equilibrium lattice parameter (\(a_0\)), bulk modulus (\(B_0\)), and the pressure derivative of bulk modulus (\(B'_0\)) for fcc Li, Na, K, Rb, and Cs, respectively. Previous theoretical calculations (Refs. 4, 22, 31, and 32) and the experimental results (Refs. 3, 4, and 33–35) through the fitting of equation of states are also shown for comparison.

<table>
<thead>
<tr>
<th>Alkali metals</th>
<th>(a_0) (a.u.)</th>
<th>(B_0) (GPa)</th>
<th>(B'_0)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Li FP</td>
<td>8.17</td>
<td>13.63</td>
<td>3.55</td>
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<tr>
<td>Li PP</td>
<td>8.15</td>
<td>15.23</td>
<td>2.66</td>
</tr>
<tr>
<td>Li Ref. 31</td>
<td>8.08</td>
<td>13.76</td>
<td>3.28</td>
</tr>
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<td>8.29(^a)</td>
<td>13.10(^b)</td>
<td>2.80(^b)</td>
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<tr>
<td>Li FP</td>
<td>10.01</td>
<td>7.43</td>
<td>3.86</td>
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<tr>
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<td>9.85</td>
<td>10.79</td>
<td>2.64</td>
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<td>6.43(^c)</td>
<td>3.84(^c)</td>
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<tr>
<td>Na FP</td>
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<td>4.4</td>
<td>4.1</td>
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<tr>
<td>K Expt.</td>
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<td>4.25(^d)</td>
<td>3.63(^d)</td>
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<tr>
<td>K FP</td>
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<tr>
<td>Cs Expt.</td>
<td>14.71(^e)</td>
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</tr>
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</table>

\(^a\)Reference 33
\(^b\)Reference 3.
\(^c\)Reference 4.
\(^d\)Reference 34.
\(^e\)Reference 35.

modulus (\(B_0\)), and the pressure derivative (\(B'_0\)) within PP and FP methods together with other theoretical results and the experimental data are listed in Table I. The theoretical lattice constants are in good agreement with experimental data within 1.4%, 3.5%, 0.8%, 4.3%, and 0.9% for Li, Na, K, Rb, and Cs, respectively. The calculated EOS of alkali metals in fcc structure within PP and FP methods are compared with the experimental data\(^3,4,33–35\) as shown in Fig. 1. The agreement between theory and experiment is excellent for Li and Na. Therefore, the current PP and FP calculations at the same volume will produce almost identical pressure for Li and Na. Note that the PP EOS for K, and the FP EOSs for Rb and Cs agree also well with the experimental measurements. However, there are some noticeable discrepancies between theory and experiment for FP calculation in K, and PP calculations in Rb and Cs. Specifically, the FP EOS in K overestimates an experimental pressure of \(-2\) GPa, while the PP results in Rb and Cs underestimate the experimental pressures of \(-2\) GPa and \(-0.5\) GPa, respectively. Therefore, all the calculated pressures below within FP theory in K and PP theory in Rb and Cs will be corrected with pressures of \(-2\), 2, and 0.5 GPa, respectively, to guarantee the current FP and PP calculations producing exactly the experimental pressures.

The evolution of two-dimensional (2D) sections of the Fermi Surface (FS) with pressure is explored on the reciprocal lattice planes (001) and (110) in the first BZ. These choices are guided by the observed significant changes in the band structures near the Fermi level along \(\Gamma-K-W-X\), \(\Gamma-X\), and \(\Gamma-L\) directions for Li, K, Rb, and Cs\(^16,32,36\) at high pressure. Figure 2 summarizes the change of the FS with pressure for Li. At zero pressure, the perfect circular feature in the 2D FS in both the (001) and (110) planes indicates a nearly free electron character. At increased pressure, while there is no noticeable change in the FS in the (100) plane (bottom row of Fig. 2), the circular feature in the (110) plane which includes the \(\Gamma, L, \) and \(K\) points (top row of Fig. 2) starts to distort at 10 GPa and finally disappears. This observation indicates that a free electron description of Li is no longer valid at very high pressure. It is significant that at 30 GPa, the FS develops into two parallel planes with a nesting vector of 0.71 (110) along the \(\Gamma-K\) direction. A FSN suggests the possibility of a structural instability which might be related to the observed structural phase transition from fcc to \(R-3m\). The predicted FSN of Li at 30 GPa is in excellent agreement with the results reported in Refs. 14 and 22.

The calculated evolution of the 2D FS with pressure for Na is shown in Fig. 3. With increasing pressure, the FS shows negligible change in both reciprocal lattice planes. Incidentally, the nearly free electron model seems still to be valid for Na even up to 105 GPa.

Figure 4 displays the change of the 2D FS with pressure for fcc K. It is found that the spherical FS is destroyed with increasing involvement of localized 3d orbital with increasing pressure. In the (110) plane the 2D FS shows a FSN feature at 8 GPa, indicating a possible structural instability for the fcc structure. At 11 GPa, the parallel FS feature starts to vanish. The electronic instability due to FSN might be related to the reversible phase transition of fcc \(\rightarrow bcc\) under uncompressing. Concerning the contrasting behavior observed in Li, we have carefully re-examined the FS and phonon calculations. We observed no hint of both dynamical and electronic stability at low pressure for Li. The reverse fcc \(\rightarrow bcc\) transition in Li therefore is not driven by phonon and electronic instability but rather by the energetic. It is significant that at 18 GPa, a second FSN feature for K appeared in the (100) plane with parallel FS along the \(\Gamma-K\) direction with a nesting vector of 0.58 (110) along the \(\Gamma-K\) direction. A FSN suggests the possibility of a structural instability which might be related to the observed structural phase transition of fcc \(\rightarrow bcc\) under uncompressing. The appearance of the FSN feature at 18 GPa coincides with the observed structural phase transition pressure of 19 GPa from fcc to the host-guest composite structure for K\(^10\). In addition, we also explore the 2D FS parallel to the \(\Gamma X K\) plane. The results are plotted in Fig. 5. It is very interesting to note that at \(-0.61\)X [Fig. 5(e)], possible nesting of the FS parallel to the \(\Gamma\) direction is predicted. The more complex FS of K reveals that there are more possibilities of electronic instability other than just in the [110] direction, as observed in Li\(^23\).

Figures 6 and 7 show the development of the 2D FS with pressure for Rb and Cs, respectively. The evolution of the FS topology for Rb and Cs is very similar to that predicted for...
K. It is important that in the (110) plane, FSN characters appeared at 3 GPa and 0 GPa, but disappeared at 6 GPa and 1 GPa for Rb and Cs, respectively. The predicted FSN in (110) plane for Rb and Cs might also be related to the reversible phase transition of fcc \( \rightarrow \) bcc when the pressure was released. New FSN features in the (100) plane for Rb and Cs are predicted at 13.2 GPa and 4 GPa, respectively. The estimated nesting vectors are all 0.58 (110) for Rb and Cs. It should be pointed out that the predicted pressures on the appearance of the FS instabilities are very close to the observed phase transition pressures of 13 GPa and 4.2 GPa for Rb and Cs from fcc to the more complex C\( \bar{2}2\bar{1} \) structures. Note also that the extended 2D FS (not shown) parallel to the \( \Gamma X K \) plane for Rb and Cs at 13.2 GPa and 4 GPa, respectively, are almost identical to that of K plotted in Fig. 5.

Figure 8 shows the calculated angular momentum decomposed DOS divided by total DOS at Fermi level for fcc Li, Na, K, Rb, and Cs with volume. From the analysis of the partial DOS in Fig. 8(b), it is shown that at zero pressure, the 3p orbital for Na is occupied at about 50% in fcc structure. With increasing pressure it increases slowly up to the border line of fcc/post-fcc. When the pressure is increased beyond 103 GPa (\( V/V_0=0.29 \)), the 3d orbital starts to become significant. This observation is in good agreement with the report of Neaton and Ashcroft. To obtain further information on the electron topology, variation of the 3D FS with pressure is also studied. It was also found that the almost spheri-

![FIG. 1. (Color online) Comparison of the calculated equation of states (solid line) for the fcc Li (a), Na (b), K (c), Rb (d), and Cs (e) with the experimental data (solid square symbols). The red lines are the results from FP method and the black lines are the results from PP method.](image1)

![FIG. 2. Fermi surface cross sections of fcc Li at 0, 10, and 30 GPa along (110) (upper panel) and (100) (lower panel) planes. Although the Fermi surface along the (100) plane shows an almost perfect circle, it becomes highly distorted in the (110) plane with a clearly nesting along the \( \Gamma - K \) direction at 30 GPa. The arrows represent nesting vectors.](image2)

![FIG. 3. Fermi surface cross sections of fcc Na at 0 and 105 GPa along (110) (upper panel) and (100) (lower panel) planes. With increasing pressure, there are no noticeable changes in FS for both planes.](image3)
The cal nature of the FS does not change at 105 GPa, even up to 242 GPa. From Fig. 8, one observes that in Li, the $p$-DOS contribution in the fcc structure is already very significant (80%) even at low pressure (large volume) and increase steadily at the expense of decreasing $s$ character. The increased $p$ contribution eventually led to the formation of a hole in the FS near the L point. In contrast, in Na, although the $s$ contribution at low pressure in the stability region of the bcc phase decreases, the $p$ contribution remains largely the same at 55%. More importantly, the $p$ contribution in the fcc phase (from $V/V_0=0.346–0.29$) is almost constant at 57% to the total DOS, while the $d$ contribution increases slightly but remains small. For this reason, there is only minor distortion in the FS near the observed phase transition at 105 GPa. This might be the reason for the persistence of the spherical FS in Na at high pressure up to 105 GPa. It is noteworthy that the significant differences in FS between Na and Li under high pressure might also be attributed to differences in the valence-core interactions. For the heavier K, Rb, and Cs in Figs. 8(c)–8(e), we indeed observed that at the pressure close to the FSN, the $d$-DOS increases significantly. It should also be pointed out that the current calculations for partial DOS in K and Rb are in excellent agreement with the previous calculation by Shi and Papaconstantopoulos.

Preliminary phonon dispersion calculations were performed with the force constant interpolation method using the linear response approach. Phonon softening is identified for all the alkali metals along the $\Gamma$-K direction at high pressures. The calculated results agree well with those reported in Refs. 14 and 15 for Li, in Ref. 16 for K, and in Ref. 22 for Cs. To obtain very accurate phonon dispersion, phonon frequencies for individual $q$ points along the $\Gamma$-K direction were calculated explicitly to eliminate possible interpolation errors in the force constant method. Figure 9 shows the directly calculated phonon results with pressure for Li, Na, K, Rb, and Cs, respectively. It is quite clear that with increasing pressure all the five alkali metals with the fcc structure show TA phonon softening that may induce structural instability. Imaginary phonon modes for Li, Na, K, Rb, and Cs start to appear at 33 GPa, 103 GPa, 28 GPa, 17 GPa, and 4 GPa, respectively. The predicted pressures correlate nicely with the experimentally measured structural transition pressures of 39 GPa, 103 GPa, 19 GPa, 13 GPa, and 4.2 GPa in fcc Li, Na, K, Rb, and Cs, respectively. For a summary, Table II lists...
soft phonon was found to occur near the zone center with an
different from that for Li, Na, and K. For Rb and Cs, the
softening behaviors for Rb at wave vectors 0.3
review for the readers. We found two distinct phonon-
measurements for these five alkali metals to provide a full
all the calculated FSN and dynamic instability features, to-
gether with previously theoretical results and experimental
measurements for these five alkali metals to provide a full
pressure for TA phonon modes
respectively.

It is very important to note that the nature of the pressure-
induced phonon softening predicted for Rb and Cs is quite
different from that for Li, Na, and K. For Rb and Cs, the
soft phonon was found to occur near the zone center with an
incommensurate softening vector of (0.3, 0.3, 0). The slopes
of phonon dispersions when \( q \rightarrow 0 \) are related to the elastic
constants of a material. For a fcc solid, when \( q \rightarrow 0 \) along
the (110) direction \( \mu_{T} = (C_{11}-C_{12})/2 \), \( \mu \) is the atomic
density, \( u_{T} \) = \( \text{d} \omega_{T}/\text{d} q \), \( \omega_{T} \) = \( 2 \pi \nu_{T} \) (\( \nu_{T} \) is TA phonon frequency). In the
case of fcc Rb, the TA phonons along [110] soften and
become imaginary at 17 GPa [Fig. 9(d)]. At this pressure,
the tetragonal shear elastic constant \( C' \) = \( (C_{11}-C_{12})/2 \) becomes
negative. This observation is similar to that found in Cs
earlier. It is significant to point out that the present theoretical
results of the similar phonon softening and the FSN be-
havior shown in Figs. 6 and 7 parallel the experimental ob-
servations on the similar phase transition sequence from fcc
(Fm-3m) to C2221 in Rb and Cs.

In contrast, for fcc Li, Na, and K, the TA phonon fre-
cuencies along [110] soften and become imaginary fre-
quency at similar incommensurate softening vectors of
\(~0.65, 0.65, 0\) or \(0.6, 0.6, 0\) near the K symmetry point
with increasing pressure [Figs. 9(a)–9(c)] as listed in Table II.
Since the phonon instabilities do not occur near the zone
center, consequently there is no weakening of the shear
estatic modulus \( C' \). The apparent difference in the pressure-
induced phonon softening behavior between heavier alkali
(Rb and Cs) and lighter alkali (Li, Na, and K) shed strong
light on the reason behind the different high-pressure
structures. It is clear that Li, Na, and K take a different route to
the pressure-induced post-fcc phases than those of Rb and Cs.
Very recently, McMahon et al. observed that fcc K
transforms to a host-guest composite structure comprising
the same 16-atom host structure as Rb-IV and a
C-face-centered, rather than a body-centered, tetragonal,
guest structure. On the other hand, fcc Li transforms to a
rhombohedral cell containing one atom with a space group of
R-3m. For fcc Na, Hanfland et al. observed a phase transition
to a low-symmetry structure at pressures beyond
103 GPa. This structure was suggested to be a body-centered
cubic structure with space group of I-43d. So far, there is

FIG. 8. (Color online) The calculated angular momentum de-
composed DOS divided by total
DOS at Fermi level for FCC Li,
Na, K, Rb, and Cs with volume
using FP method. The dashed line
is the phase border.

FIG. 9. (Color online) Calculated phonon dispersions of fcc Li
(a), Na (b), K (c), Rb (d), and Cs (e) along the \( \Gamma-K \) direction with
pressure for TA phonon modes (frequencies below the zero axis
denote imaginary values). The phonons become unstable around the
K symmetry point at 33 GPa for Li, 103 GPa for Na and 28 GPa for
K, and near the zone center at 17 GPa for Rb and at 4 GPa for Cs,
respectively.
TABLE II. Calculated phonon softening wave vectors \( \mathbf{q} \) and transition pressures \( P^E_i \), and FSN wave vectors \( \mathbf{P}^R_i \) and transition pressures \( P^F_i \) for fcc Li, Na, K, Rb, and Cs, respectively. Previous theoretical calculations (Refs. 15 and 22) on phonon softening wave vectors \( \mathbf{q} \) and transition pressures \( P^E_i \) for Li and Cs, and the experimental measurements (Refs. 4, 5, 9, 11, and 12) on the phase transition pressures for five alkali metals are shown for comparison. The experimentally measured (Refs. 9–12) post-fcc structures for Li, K, Rb, and Cs, and the proposed (Ref. 13) post-fcc phase structures for Na are also listed.

<table>
<thead>
<tr>
<th>Experimental observations</th>
<th>Phonon instability</th>
<th>Fermi surface nesting</th>
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<tr>
<td><strong>Post-fcc phases</strong></td>
<td><strong>Wave vector</strong></td>
<td><strong>Wave vector</strong></td>
</tr>
<tr>
<td></td>
<td>( q (2\pi/a_0) )</td>
<td>( P^E_i ) (GPa)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>( P^F_i ) (GPa)</td>
</tr>
<tr>
<td>Li</td>
<td>( 0.7, 0.7, 0 )</td>
<td>33</td>
</tr>
<tr>
<td></td>
<td>( 0.65, 0.65, 0 )</td>
<td>35</td>
</tr>
<tr>
<td>Na</td>
<td>( 0.6, 0.6, 0 )</td>
<td>103</td>
</tr>
<tr>
<td>K</td>
<td>( 0.6, 0.6, 0 )</td>
<td>31</td>
</tr>
<tr>
<td>Rb</td>
<td>( 0.3, 0.3, 0 )</td>
<td>17</td>
</tr>
<tr>
<td>Cs</td>
<td>( 0.3, 0.3, 0 )</td>
<td>4</td>
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</table>

\( a \)Reference 9.
\( b \)Reference 11.
\( c \)Reference 5.
\( d \)Reference 10.
\( e \)Reference 15.
\( f \)Reference 11.
\( g \)Reference 4.
\( h \)Reference 12.
\( i \)Reference 10.

Among the alkali metals, high-pressure post-fcc structures have only been unambiguously determined for Li, K, Rb, and Cs. With the limited experimental results in combination with the current calculations, we can make the following remarks. Besides for Na, it is also proposed that the TA phonon softening is responsible for the phase transition in fcc Li. A phonon-driven fcc → rhombohedral transformation follows the normal sequence of high-pressure transformation. Rhombohedra is a subgroup of hexagonal and therefore the general sequence for increasing dense packing bcc → fcc → hexagonal is followed. Furthermore, a shear instability can easily distort an fcc unit cell into a rhombohedral structure. The situation in Rb and Cs is more complicated. There is obviously a competition between FSN and phonon softening instabilities. If FSN indeed drives the transition, it will be likely analogous to a charge density wave distortion (CDW) resulting in a modulated structure.20 Both Rb and Cs transform to the \( C_{222_1} \) structure but with different stacking of atomic layers along the \( c \) axis before reaching more regular and simplistic tetragonal \( I_4_{1/amd} \) structure at higher pressure. The observed modulation in atomic layers for Rb and Cs within \( C_{222_1} \) structure is a strong hint of CDW distortion. It is noteworthy that the post-fcc structures for Li, \( R-3m \) and cI16 are not modulated.

In conclusion, the FS and phonon lattice dynamics at high pressure fcc alkali metals have been investigated extensively using \textit{ab initio} method within the density functional theory. Fermi surface nesting along \( \Gamma-K \) in the Brillouin zone is identified for Li with a nesting vector of 0.71 (110), K, Rb, and Cs with a nesting vector of 0.58 (110), while no distortion of the free-electron-like FS for Na was found. A TA phonon softening along \( \Gamma-K \) with pressure is predicted for all.
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